



Full length article



Strain effect on the intraband absorption coefficient for spherical CdSe/CdS/ZnSe core–shell–shell quantum dots

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ABSTRACT

In this work, we theoretically calculated the intraband absorption coefficient (IAC) between the $1s$ and $1p$ conduction band states for a spherical core/shell/shell quantum dot (CSS-QD) as function of inner and outer shells' sizes with and without the presence of strain effect. The electronic structure for the system is computed in the effective mass approximation framework and the strain effect is considered on the continuum elasticity model. We found out that as we compared the strained and the unstrained system, the former causes that the IAC undergoes a small redshift. A similar behavior occurs as the inner and outer shell size increase. The results show that the strain effect is an important factor that will be considered in these nanostructure type. The incorporation of inner and outer shells allowed us to extend some fractions of eV into the absorption spectrum that could be interesting as a mechanism to control the IAC device design.

1. Introduction

The semiconductor quantum dots (QDs) have attracted much attention due to the several device applications [1–4] particularly the related ones with the optical properties. Molecular Beam Epitaxy (MBE), Metal-Organic Chemical Vapor Deposition (MOCVD), and in general the synthesis by chemical methods allow the experimentalist to grow semiconductor QDs with several geometries. In this regard, the core–shell quantum dots (CS-QDs) system is experimentally feasible and basically consist of a spherical QD of some semiconductor material (which in this case represents the core) covered by another semiconductor material, commonly known as a shell. Recently, Young-Shin Park et al. [5] published a report that assets that the optical properties can be easily controlled by the quantum confinement and probably, among several possible applications, the colloidal QD lasers reflects the accumulated knowledge on the QDs, the CS-QDs also included. Typically, the CS-QDs are compound by II–VI, III–V, and IV–VI semiconductor materials, and the physical properties depends on the band-gaps and the band offsets as well as on the lattice mismatch because the heterostructure could be type-I or -II and the strain effect could also of paramount importance on the optoelectronic properties.

Several authors have theoretically studied III–V CS-QDs, they mainly reported that the optical properties strongly depends on the QD size

and on the shape of the confinement potential, as well as on the incorporation of donor impurities, the presence of electric and magnetic fields and by hydrostatic pressure effects [6–21]. On the other hand, II–VI core–shell and core–shell–shell QDs composed by semiconductors as CdSe/CdS, CdSe/HgS, CdSe/PbS, ZnSe/ZnSe, ZnS/CdS, CdSe/CdS/ZnS, CdSe/ZnSe/ZnS and CdTe/CdS/ZnS have been also reported by experimental researchers [22–24]. When semiconductors with different lattice parameters are in contact, a lattice mismatch in the interface is present and consequently, an elastic strain effect is part of the system. The strain has a vital role on the physical properties for the semiconductor heterostructure. A.M. Smith et al. [25] experimentally found that the strain effect clearly modifies the electronic band structure, and consequently it affects the optical properties. Theoretically, the core–shell ZnTe/ZnSe, and CdTe/ZnSe QDs strain is reported by T.O. Cheche et al. [26,27], they considered the shell's size to change the electronic properties. Strain studies on the inter-band absorption coefficient and photo-excited carrier localization are also calculated in CdSe/CdS/ZnS, ZnTe/ZnSe/ZnS CSS-QDs by T.E. Pahomi and coworkers [28]. Theoretical comparison of the electron and hole states, and the emission spectrum of InP/ZnSe/ZnS and CdSe/ZnSe/ZnS heterostructures were investigated [29]. Recently, the size dependent strain effect in the

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conversion efficiencies (CE) for a CS-QD is studied in [30,31], the results show that the strain effect has a very important influence on the CE. Model solid theory [32] and continuum elasticity model (CM) [28] have been used to determinate the strain effects.

Related with the strain effect, there are theoretical works where different approaches have been used to calculate the electronic structure [33–35]. Optical properties are reported by different authors also. For instance, R. Kostić and D. Stojanović [36] calculated the oscillator strengths and report the intersubband optical absorption coefficient considering third-order nonlinear contributions in a CdSe/ZnS/CdSe/SiO₂ spherical QD. The optical absorption coefficient (OAC) is obtained in CdSe/CdS/CdSe/CdS, CdSe/Pb_{1-x}Cd_xSe/CdSe, CdSe/ZnTe, CdSe/ZnS CS-QDs in Refs. [37–40]. In these works, we can see that the OAC strongly depends on the size and composition semiconductor materials of CS-QDs. An important study of the absorption coefficient of CdSe/ZnS and ZnS/CdSe CS-QD in the case of luminescent solar concentrators (LSCs) is conducted by Bahareh et al. [41], their results show that the CS-QDs can absorb higher energy photons in solar spectrum in comparison with the inverted CS-QDs. In the previous works, interesting results are shown for CS-QDs systems, however, it is also possible to have another shell, so we considered the strain effect in a CdSe/CdS/ZnSe CSS-QD as function of the shells' sizes. The importance of this contribution is that we considered the strain effect, by working within the effective mass theory, for the case of CdSe/CdS/ZnSe spherical quantum dot following the lines of T.E. Pahomi [42]; additionally, it is relevant to say that core/shell and core/shell/shell spherical heterostructures are experimentally feasible. The aim of this study is to exhibit how the intraband absorption coefficient could be tuned in different regions of the absorbed photon energy. The study is carried out within the effective mass approximation, considering parabolic bands, and the strain effect is considered by the model solid theory and continuum elasticity model.

The organization of the paper is the following: Section 2 describes the studied system and the theoretical used model to calculate the electronic and intraband absorption coefficient. Section 3 shows the results of the electronic states, energies and intraband absorption coefficient as a function of shell's sizes. The conclusions are finally presented in Section 4.

2. Theoretical framework

In this work, we theoretically studied the intraband absorption coefficient for a spherical CSS-QD composed by a CdSe core, covered with inner and outer shells of CdS and ZnSe semiconductor materials, respectively. The main transition is considered between the 1s and 1p electron states. A schematic representation of the CSS-QD is presented in Fig. 1. Here r_{CdSe} , w_{CdS} , and w_{ZnSe} are the core radius and the inner and outer shells widths.

The electronic structure is calculated by a finite difference method within the framework of the effective mass approximation. The confined energies and the wave functions for the electronic states are obtained by the BenDaniel–Duke equation [43]

$$\left[-\frac{\hbar^2}{2} \nabla \cdot \left(\frac{1}{m^*} \nabla \right) + V(\vec{r}) \right] \psi(\vec{r}) = E \psi(\vec{r}), \quad (1)$$

where \hbar is the reduced Planck constant, m^* is the isotropic electron effective mass in each region, $V(\vec{r})$ is the confinement potential, E are the energy level spectrum and $\psi(\vec{r})$ stands for the envelope function.

For the CSS-QD, we considered a spherical symmetry, such that we can separate the envelope function in angular and radial components:

$$\psi(r, \theta, \phi) = R_{n\ell} Y_{\ell}^m(\theta, \phi), \quad (2)$$

being $R_{n\ell}$ the radial wave function and $Y_{\ell}^m(\theta, \phi)$ the well known spherical harmonics. The radial wave functions are calculated by

$$\left[-\frac{\hbar}{2} \frac{d}{dr} \left(\frac{1}{m^*} \frac{d}{dr} \right) + \frac{\ell(\ell+1)\hbar^2}{2m^*r^2} + V(r) \right] U_{n\ell}(r) = E U_{n\ell}(r), \quad (3)$$

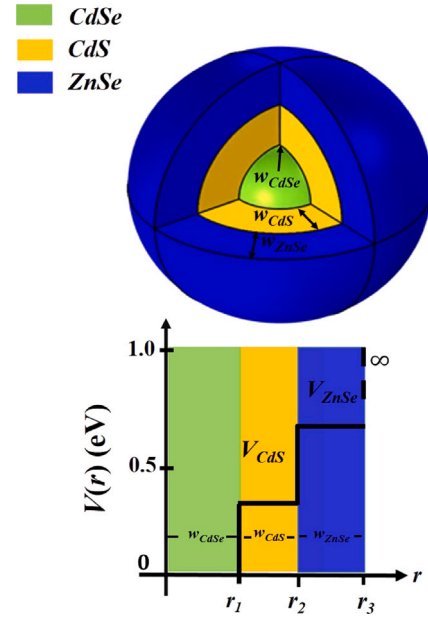


Fig. 1. CdSe/CdS/ZnSe CSS-QD schematic representation and the correspondingly confinement potential profile. The core radius and shells widths are represented as r_{CdSe} , w_{CdS} ($r_2 - r_1$) and w_{ZnSe} ($r_3 - r_2$).

where $U_{n\ell}(r) = rR_{n\ell}(r)$, and the subscripts n and ℓ label the principal and the angular quantum number, respectively. The confinement potential (Fig. 1) is given by:

$$V(r) = \begin{cases} 0, & 0 \leq r \leq r_1 \\ V_{CdS}, & r_1 < r \leq r_2 \\ V_{ZnSe}, & r_2 < r \leq r_3 \\ \infty, & r > r_3, \end{cases} \quad (4)$$

with $V_{CdS} = E_c^{CdS} - E_c^{CdSe}$ and $V_{ZnSe} = E_c^{ZnSe} - E_c^{CdS}$ and, according with the model-solid theory, the value of the strained conduction band edge is

$$E_c = E_c^0 + a_c \frac{\Delta\Omega}{\Omega} \quad (5)$$

where $E_c^0 = E_g^0 + E_v^0$ is the unstrained band edge values, a_c stands for the hydrostatic deformation potentials, $\Delta\Omega/\Omega$ represents the fractional volume change, also denoted as ε_{hyd} .

According to the expressions obtained by T.E. Pahomi [42], the ε_{hyd} within the continuum elasticity approach, for the radial displacement, is described by

$$\varepsilon_{hyd}^{CdSe} = 2 \frac{1 - 2\nu_{CdSe}}{1 - \nu_{CdSe}} \left[\varepsilon_1 \left(1 - \frac{r_1^3}{r_3^3} \right) + \varepsilon_2 \left(1 - \frac{r_2^3}{r_3^3} \right) \right], \quad (6)$$

$$\varepsilon_{hyd}^{CdS} = 2 \frac{1 - 2\nu_{CdS}}{1 - \nu_{CdS}} \left[-\varepsilon_1 \frac{r_1^3}{r_3^3} + \varepsilon_2 \left(1 - \frac{r_2^3}{r_3^3} \right) \right], \quad (7)$$

$$\varepsilon_{hyd}^{ZnSe} = -2 \frac{1 - 2\nu_{ZnSe}}{1 - \nu_{ZnSe}} \left(\varepsilon_1 \frac{r_1^3}{r_3^3} + \varepsilon_2 \frac{r_2^3}{r_3^3} \right), \quad (8)$$

where the superscripts CdSe, CdS and ZnSe represent the core and the shells regions, respectively, $\varepsilon_{1(2)}$ are the relative mismatch defined as

$$\varepsilon_{1(2)} = \frac{a_{CdS(ZnSe)} - a_{CdSe(CdS)}}{a_{CdSe(CdS)}}, \quad (9)$$

being ν the Poisson ratio. The intraband absorption coefficient expression, given by S.L. Chuang [44], is:

$$\alpha(\hbar\omega) = \left(\frac{\pi\omega}{n_r c \varepsilon_0} \right) \frac{2}{V} \sum_k |\vec{e} \cdot \vec{\mu}_{fi}|^2 \delta(E_f - E_i - \hbar\omega), \quad (10)$$

Table 1
Used materials parameters [28,32].

	CdSe	CdS	ZnSe
m^*	$0.15 m_e$	$0.22 m_e$	$0.21 m_e$
a (nm)	0.605	0.582	0.565
ν	0.408	0.410	0.376
E_g^0 (eV)	1.74	2.49	2.69
a_v (eV)	0.9	0.4	1.65
a_c (eV)	-2	-2.54	-4.17
E_v^0 (eV)	-6.00	-6.42	-6.07

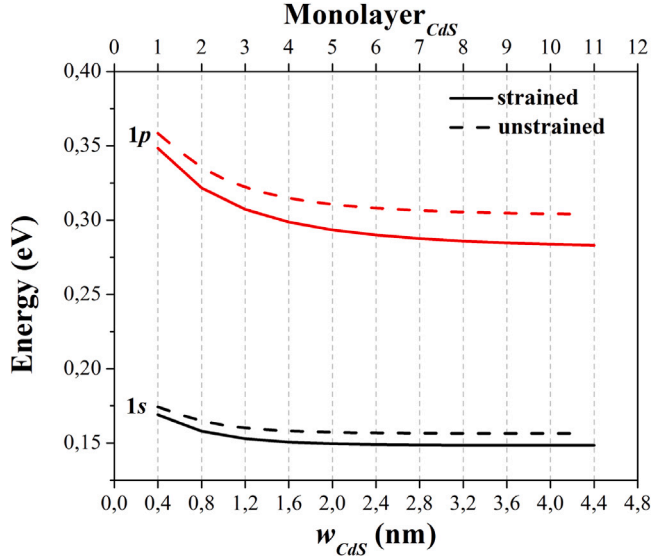


Fig. 2. 1s- and 1p-state energy levels as function of the CdS shell width (w_{CdS}) for strained (solid lines) and unstrained (dashed line) spherical CdSe/CdS/ZnSe CSS-QD. The core radius is $r_{CdSe} = 2.8$ nm and the ZnSe shell width is $w_{ZnSe} = 0.66$ nm.

here $\bar{\mu}_{fi} = \langle f | \vec{e} \cdot \vec{r} | i \rangle$ and the Dirac delta function can be represented as a Lorentzian function, as follows:

$$\delta(E_f - E_i - \hbar\omega) = \frac{\Gamma/2\pi}{(E_f - E_i - \hbar\omega)^2 + \left(\frac{\Gamma}{2}\right)^2}, \quad (11)$$

with $\Gamma = 30$ meV. The initial energy (E_i) and final one (E_f) corresponds to the 1s- and 1p-state, respectively, and $\hbar\omega$ stands for the incident photon energy. Here we use $\Delta m = 0$ and considered a linear z-polarization, so that,

$$\langle f | \vec{e} \cdot \vec{r} | i \rangle = \int \{ Y_1^0(\theta, \varphi) R_{11}(r) \}^* r \cos \theta Y_0^0(\theta, \varphi) R_{00}(r) r^2 \sin \theta dr d\theta d\varphi, \quad (12)$$

where Y_ℓ^m are the well known spherical harmonics [45].

3. Results and discussion

In this section, we present the computations of the strain effect in the electronic structure and intraband optical absorption coefficient for a spherical CSS-QD composed by a CdSe core, CdS inner shell and ZnSe outer shell, as represented in Fig. 1. The lattice mismatches values are $\varepsilon_1 = 0.038$ and $\varepsilon_2 = 0.029$. We used a core radius of 2.8 nm because the system begun to confine two states (the 1s and 1p). Table 1 contains the material's parameters used in the calculations.

Fig. 2 shows the 1s- and 1p-state energy levels as function of the CdS shell width w_{CdS} from 0.4 to 4.4 nm (1–11 monolayers) for strained (solid lines) and unstrained (dashed lines) spherical core-shell-shell CdSe/CdS/ZnSe quantum dot. The CdSe core radius (r_{CdSe}) and ZnSe shell width (w_{ZnSe}) are fixed to 2.8 and 0.66 nm, respectively. We can

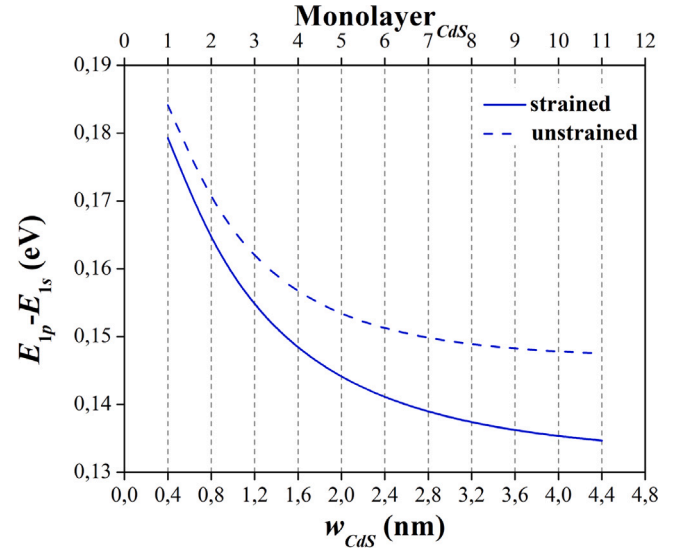


Fig. 3. Main energy difference between the 1s- and 1p-state energy levels as function of the CdS shell width (w_{CdS}). The CdSe core radius is $r_{CdSe} = 2.8$ nm while the ZnSe shell is $w_{ZnSe} = 0.33$ nm.

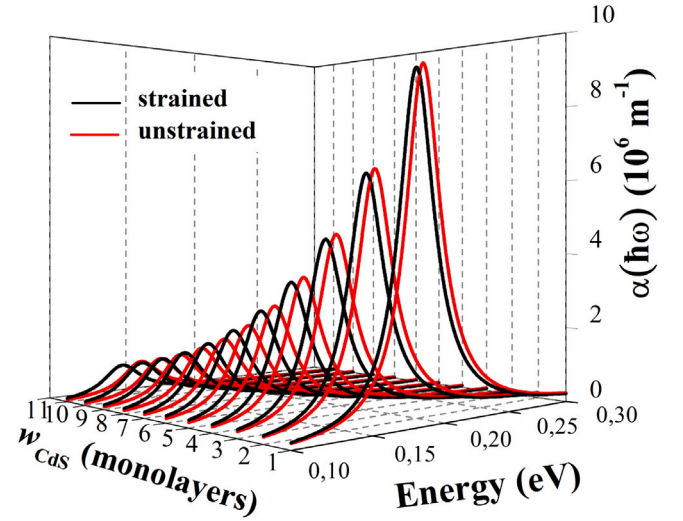


Fig. 4. Intraband absorption coefficient as function of the incident energy photon for spherical CdSe/CdS/ZnSe CSS-QD for w_{CdS} from 0.4 to 4.4 nm, with $r_{CdSe} = 2.8$ nm and $w_{ZnSe} = 0.33$ nm. The red and black line represents unstrained and strained quantum dot, respectively.

notice that the energy levels diminished as w_{CdS} increases, and the ground state (1s-state) is almost flat starting from w_{CdS} about 2.4 nm. The energy values of the strained system are lower than those that corresponds to the unstrained system.

In Fig. 3, the energy difference ($E_{1p} - E_{1s}$) between the 1s- and 1p-state, for strained and unstrained systems is presented. $E_{1p} - E_{1s}$ behavior is alike as that exhibit for each state in Fig. 2, but we must stress that the consideration of the strain effect give a lower energy difference in comparison with unstrained system. The strained and the unstrained CSS-QD energy difference range are 0.179–0.135 eV and 0.184–0.147 eV, respectively. We can see that the strain importantly affected the energy levels difference and consequently will be reflected in the intraband absorption coefficient peak location, as will be discussed below.

Intraband absorption coefficient as function of the incident-photon energy for the same configuration, as in Fig. 2, is presented in Fig. 4.

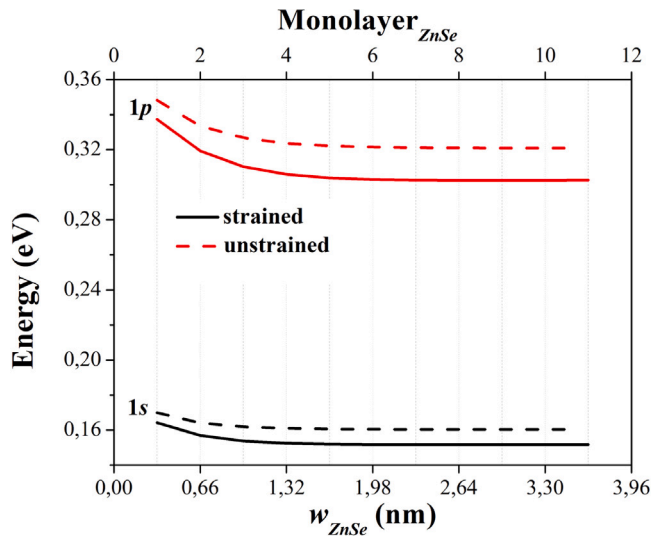


Fig. 5. 1s- and 1p-state energy levels as function of the outer shell size w_{ZnSe} for a strained (solid line) and unstrained (dashed line) spherical CdSe/CdS/ZnSe CSS-QD. The core radius is $r_{CdSe} = 2.8$ nm and the CdS inner shell is $w_{CdS} = 0.8$ nm.

Black and red lines represent the strained and unstrained CSS-QD configurations, respectively. By comparing the strained and the unstrained system, we can notice that the IAC resonant peak locates in lower energies (or has a redshift), the same situation occurs when the w_{CdS} increases, these results are consistent with the results in Fig. 3 computations, as predicted above. The intensity in the IAC decrease as w_{CdS} rises due to its dependence on $1/V$.

Fig. 5 reported the 1s (black lines) and 1p (red lines) energy levels as function of the outer shell size w_{ZnSe} (ranging within 1–3.63 nm or 1–11 monolayers) for a strained (solid lines) and unstrained (dashed lines) CdSe/CdS/ZnSe QD, with a core radius of $r_{CdSe} = 2.8$ nm and the CdS inner shell $w_{CdS} = 0.8$ nm. The behavior of the energy levels are alike to those shown as function of the inner shell width w_{CdS} . However, they are in different energy region, determined by the chosen parameters. But the most important fact is that the energy levels become unaffected (flat) for outer shell sizes (w_{ZnSe}) starting from 6 monolayers (about 1.98 nm) for the 1s-state and from 7 monolayers (about 2.31 nm) for the 1p-state, that means that the outer shell can modify the energy levels structure for values of w_{ZnSe} smaller than 2.5 nm, approximately. The energy difference between the 1s- and 1p-state is shown in Fig. 6, and as the w_{ZnSe} rises, the $E_{1p} - E_{1s}$ decreases.

Finally, in Fig. 7 we present the intraband absorption coefficient as a function of the incident photon energy for the spherical CdSe/CdS/ZnSe QD, w_{ZnSe} from 0.33 to 3.3 nm, with $r_{CdSe} = 2.8$ nm and $w_{CdS} = 0.8$ nm. The resonant peak of the IAC for the strained system exhibits a redshift respect to the unstrained system and as the w_{ZnSe} increases. The redshift can easily be understood with results of Fig. 6 because, as discussed above, the main energy difference is lower for strained than for unstrained system. In fact, the redshift for $w_{ZnSe} = 0.33$ nm is about 0.004 eV and as w_{ZnSe} increases it reaches almost 0.010 eV. Once again the diminishing in the magnitude of the intraband absorption coefficient obeys the $1/V$ dependency from Eq. (10), because as the outer shell width increases, the volume of the CSS-QD also augment.

4. Conclusions

In this work, we have investigated the electronic structure and the intraband absorption coefficient under the presence of the strain effect. The main conclusion of this work is that the strain effect represent a small but important factor in the calculated electronic and optical

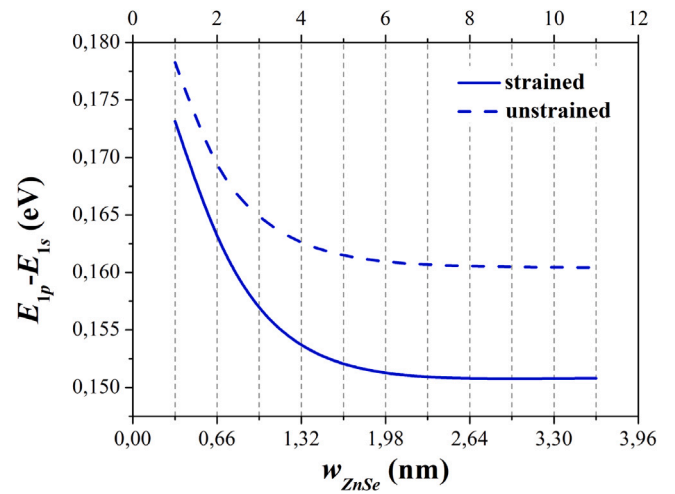


Fig. 6. Energy difference between the 1s and 1p energy levels as function of w_{ZnSe} . The core radius and the inner shell size is $r_{CdSe} = 2.8$ nm and $w_{CdS} = 0.8$ nm, respectively.

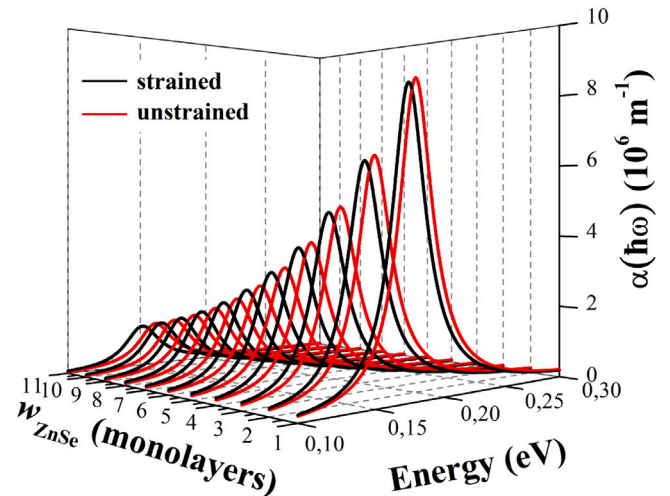


Fig. 7. Intraband absorption coefficient as function of the incident photon energy for spherical CdSe/CdS/ZnSe CSS-QD for when the outer shell size (w_{ZnSe}) increases from 0.33 to 3.3 nm. $r_{CdSe} = 2.8$ nm and $w_{CdS} = 0.8$ nm.

properties. The unstrained and strained system was compared and the results shown that the strain effect causes a redshift from 3% to 8% in the electronic states and in the IAC. As the inner and outer shell sizes augmented, the intraband absorption coefficient undergoes a redshift about 0.044 and 0.037 eV, respectively. The CdSe/CdS/ZnSe quantum dot exhibits a higher absorption range that of the CSS-QDs III–V counterpart. From the theoretical point of view, this methodology can be used to study other II–VI heterostructures, since it considers the deformation effect on spherical symmetries within the effective mass theory and the standard elasticity theory. In fact, the idea of theoretically comparing the study with and without deformation was to emphasize the importance of correctly characterizing the heterostructures that are naturally deformed, due to the difference in the lattice constant between materials. From the applied point of view, these studies help to design core/shell or core/shell/shell quantum dots by predicting the interband absorption coefficient of light, and varying the barrier widths and heights at will. These calculations can give experimenters information to synthesize quantum dots with desired properties.

CRedit authorship contribution statement

K.A. Rodríguez-Magdaleno: Conceptualization, Validation, Software, Methodology, Writing – original draft. **R. Pérez-Álvarez:** Methodology, Validation, Writing – review & editing. **F. Ungan:** Writing – review & editing, Validation, Methodology. **J.C. Martínez-Orozco:** Funding acquisition, Methodology, Project administration, Software, Validation.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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